Baby Step, Giant Step

HackerRank

You are standing at point (0,0) on an infinite plane. In one step, you can move from some point (x_f, y_f) to any point (x_t, y_t) as long as the Euclidean distance, $\sqrt{(x_f - x_t)^2 + (y_f - y_t)^2}$, between the two points is either a or b. In other words, each step you take must be exactly a or b in length.

You are given q queries in the form of a, b, and d. For each query, print the minimum number of steps it takes to get from point (0,0) to point (d,0) on a new line.

Input Format

The first line contains an integer, q, denoting the number of queries you must process.

Each of the q subsequent lines contains three space-separated integers describing the respective values of a, b, and d for a query.

Constraints

- $1 \leq q \leq 10^5$
- $1 \le a < b \le 10^9$
- $0 \le d \le 10^9$

Output Format

For each query, print the minimum number of steps necessary to get to point (d, 0) on a new line.

Sample Input 0

Sample Output 0

2 0 3

Explanation 0

We perform the following q=3 queries:

- 1. One optimal possible path requires two steps of length a = 2: $(0,0)\overrightarrow{2}(\frac{1}{2},\frac{\sqrt{15}}{2})\overrightarrow{2}(1,0)$. Thus, we print the number of steps, 2, on a new line.
- 2. The starting and destination points are both (0,0), so we needn't take any steps. Thus, we print 0 on a new line.

3. One optimal possible path requires two steps of length b = 4 and one step of length a = 3: $(0,0)\overrightarrow{4}(4,0)\overrightarrow{4}(8,0)\overrightarrow{3}(11,0)$. Thus, we print 3 on a new line.