Day 6: Bitwise Operators

HackerRank

Objective

Today, we're practicing *bitwise operations*. Check the attached tutorial for more details.

Task

We define S to be a sequence of distinct sequential integers from 1 to n; in other words, $S = \{1, 2, 3, \ldots, n\}$. We want to know the maximum bitwise AND value of any two integers, a and b(where a < b), in sequence S that is also *less than a given integer*, k.

Complete the function in the editor so that given n and k, it returns the maximum $a \ b < k$.

Note: The & symbol represents the bitwise AND operator.

Input Format

The first line contains an integer, q, denoting the number of function calls. Each of the q subsequent lines defines a dataset for a function call in the form of two space-separated integers describing the respective values of n and k.

Constraints

- $1 \le q \le 10^3$
- $2 \leq n \leq 10^3$
- $2 \leq k \leq n$

Output Format

Return the maximum possible value of a & b < k for any a < b in sequence S.

Sample Input 0

Sample Output 0

1 4 0

Explanation 0

We perform the following q = 3 function calls:

1. When n = 5 and k = 2, we have the following possible a and b values in set $S = \{1, 2, 3, 4, 5\}$:

 $\begin{array}{ll} ab & a \ \& \ b \\ 12001 \ \& \ 010 = (000)_2 \Rightarrow (0)_{10} \\ 13001 \ \& \ 011 = (001)_2 \Rightarrow (1)_{10} \\ 14001 \ \& \ 100 = (000)_2 \Rightarrow (0)_{10} \\ 15001 \ \& \ 101 = (001)_2 \Rightarrow (1)_{10} \\ 23010 \ \& \ 011 = (010)_2 \Rightarrow (2)_{10} \\ 24010 \ \& \ 100 = (000)_2 \Rightarrow (0)_{10} \\ 25010 \ \& \ 101 = (000)_2 \Rightarrow (0)_{10} \\ 34011 \ \& \ 100 = (000)_2 \Rightarrow (0)_{10} \\ 35011 \ \& \ 101 = (001)_2 \Rightarrow (1)_{10} \\ 45100 \ \& \ 101 = (100)_2 \Rightarrow (4)_{10} \\ The maximum of any \ a \ \& \ b \ that \ is \ also < k \ is \ 1, \ so \ we \ return \ 1. \end{array}$

- 2. When n = 8 and k = 5, the maximum of any a & b < k in set $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$ is 4 (see table above), so we return 4.
- 3. When n = 2 and k = 2, the maximum of any a & b < k in set $S = \{1, 2\}$ is 0 (see table above), so we return 0.

Sample Input 1

Sample Output 1

1 2

Explanation 1

We perform the following q = 2 function calls:

- 1. When n = 9 and k = 2, the maximum of any a & b < k in set $S = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ is 1 (see table above), so we return 1.
- 2. When n = 8 and k = 3, the maximum of any a & b < k in set $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$ is 2 (see table above), so we return 2.