# Kitty's Calculations on a Tree

HackerRank

Kitty has a tree, T, consisting of n nodes where each node is uniquely labeled from 1 to n. Her friend Alex gave her q sets, where each set contains k distinct nodes. Kitty needs to calculate the following expression on each set:

$$igg(\sum_{\{u,v\}} u \cdot v \cdot dist(u,v)igg) mod (10^9+7)$$

where:

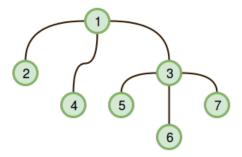
- $\{u,v\}$  denotes an unordered pair of nodes belonging to the set.
- dist(u,v) denotes the number of edges on the unique (shortest) path between nodes u and v.

Given T and q sets of k distinct nodes, calculate the expression for each set. For each set of nodes, print the value of the expression modulo  $10^9 + 7$  on a new line.

## Example

edges = [[1, 2], [1, 3], [1, 4], [3, 5], [3, 6], [3, 7]]queries = [4, 5, 7]

The graph looks like this:



There are three pairs that can be created from the query set: [4, 5], [4, 7], [5, 7]. The distance from 4 to 5 is 3, from 4 to 7 is 3, and from 5 to 7 is 2.

Now do the summation:

$$\begin{array}{l} (4 \cdot 5 \cdot dist(4,5) + 4 \cdot 7 \cdot dist(4,7) + 5 \cdot 7 \cdot dist(5,7)) \bmod (10^9 + 7) \\ \Rightarrow (4 \cdot 5 \cdot 3 + 4 \cdot 7 \cdot 3 + 5 \cdot 7 \cdot 2) \bmod (10^9 + 7) \\ \Rightarrow 214 \end{array}$$

### **Input Format**

The first line contains two space-separated integers, the respective values of n (the number of nodes in tree T) and q (the number of nodes in the query set).

Each of the n-1 subsequent lines contains two space-separated integers, a and b, that describe an

undirected edge between nodes a and b.

The  $2 \cdot q$  subsequent lines define each set over two lines in the following format:

1. The first line contains an integer,  ${m k}$ , the size of the set.

2. The second line contains  ${m k}$  space-separated integers, the set's elements. Constraints

- $1 \le n \le 2 \cdot 10^5$
- $1 \leq a, b \leq n$
- $1 \leq q \leq 10^5$
- $1 \leq k_i \leq 10^5$
- The sum of  $k_i$  over all q does not exceed  $2\cdot 10^5$  .
- All elements in each set are *distinct*.

### Subtasks

- +  $1 \leq n \leq 2000$  for 24% of the maximum score.
- +  $1 \leq n \leq 5 \cdot 10^4$  for 45% of the maximum score.
- +  $1 \leq n \leq 2 \cdot 10^5$  for 100% of the maximum score.

## **Output Format**

Print q lines of output where each line i contains the expression for the  $i^{th}$  query, modulo  $10^9+7$ .

### Sample Input 0

 7
 3

 1
 2

 1
 3

 1
 4

 3
 5

 3
 6

 3
 7

 2
 4

 1

 5

 3
 7

 2
 4

 3

 5

 3

 5

 3

 2
 4

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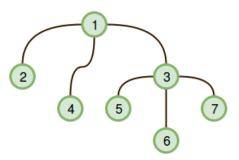
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# Sample Output 0

16 0 106		
0		
106		

# **Explanation 0**

Tree T looks like this:



We perform the following calculations for q=3 sets:

• Set 0: Given set  $\{2,4\}$ , the only pair we can form is (u,v) = (2,4), where dist(2,4) = 2. We then calculate the following answer and print it on a new line:

$$egin{aligned} (2 \cdot 4 \cdot dist(2,4)) egin{aligned} & ext{mod} \ (10^9+7) \ & \Rightarrow (2 \cdot 4 \cdot 2) egin{aligned} & ext{mod} \ (10^9+7) \ & \Rightarrow 16 \end{aligned}$$

- Set 1: Given set  $\{5\}$ , we cannot form any pairs because we don't have at least two elements. Thus, we print 0 on a new line.
- Set 2: Given set  $\{2, 4, 5\}$ , we can form the pairs (2, 4), (2, 5), and (4, 5). We then calculate the following answer and print it on a new line:

$$egin{aligned} &(2 \cdot 4 \cdot dist(2,4) + 2 \cdot 5 \cdot dist(2,5) + 4 \cdot 5 \cdot dist(4,5)) egin{aligned} & ext{mod} \ &(10^9 + 7) \ &\Rightarrow (2 \cdot 4 \cdot 2 + 2 \cdot 5 \cdot 3 + 4 \cdot 5 \cdot 3) egin{aligned} & ext{mod} \ &(10^9 + 7) \ &\Rightarrow 106 \end{aligned}$$