Palindromic Subsets

HackerRank

Consider a lowercase English alphabetic letter character denoted by c. A *shift* operation on some c turns it into the next letter in the alphabet. For example, and $shift(\texttt{a}) = \texttt{b}$, $shift(\texttt{e}) = \texttt{f}$, $shift(\texttt{z}) = \texttt{a}$.

Given a zero-indexed string, s, of n lowercase letters, perform q queries on s where each query takes one of the following two forms:

- `1 i j t`: All letters in the inclusive range from i to j are shifted t times.
- `2 i j`: Consider all indices in the inclusive range from i to j. Find the number of non-empty subsets of characters, $c_1, c_2, \ldots, c_k$ where $i \leq$ index of $c_1 <$ index of $c_2 < \ldots <$ index of $c_k \leq j)$, such that characters $c_1, c_2, c_3, \ldots, c_k$ *can be rearranged* to form a palindrome. Then print this number modulo $10^9 + 7$ on a new line. Two palindromic subsets are considered to be different if their component characters came from different indices in the original string.

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Input Format

The first line contains two space-separated integers describing the respective values of n and q.
The second line contains a string of n lowercase English alphabetic letters (i.e., `a` through `z`) denoting s.
Each of the q subsequent lines describes a query in one of the two formats defined above.

Constraints

- $1 \leq n \leq 10^5$
- $1 \leq q \leq 10^5$
- $0 \leq i \leq j < n$ for each query.
- $0 \leq t \leq 10^9$ for each query of type 1.

Subtasks

For 20% of the maximum score:

- $n \leq 500$
- $q \leq 500$

For another 30% of the maximum score:

- All queries will be of type 2.

Output Format

For each query of type 2 (i.e., `2 i j`), print the number of non-empty subsets of characters satisfying the conditions given above, modulo $10^9 + 7$, on a new line.

Sample Input 0

```
3 5
aba
2 0 2
2 0 0
2 1 2
1 0 1 1
2 0 2
```

Sample Output 0

```
5
1
2
3
```

Explanation 0

We perform the following $q = 5$ queries:

1. `2 0 2`: $s =$ **aba** and we want to find the palindromic subsets of substring **aba**. There are five such subsets that form palindromic strings (**a**, **b**, **a**, **aa**, and **aba**), so we print the result of $5 \bmod (10^9 + 7) = 5$ on a new line
2. `2 0 0`: $s =$ **aba** and we want to find the palindromic subsets of substring **a**. Because this substring only has one letter, we only have one subset forming a palindromic string (**a**). We then print the result of $1 \bmod (10^9 + 7) = 1$ on a new line.
3. `2 1 2`: $s =$ **aba** and we want to find the palindromic subsets of substring **ba**. There are two such subsets that form palindromic strings (**b** and **a**), so we print the result of $2 \bmod (10^9 + 7) = 2$ on a new line.
4. `1 0 1 1`: $s =$ **aba** and we need to perform $t = 1$ shift operations on each character from index $i = 0$ to index $j = 1$. After performing these shifts, $s =$ **bca**.
5. `2 0 2`: $s =$ **bca** and we want to find the palindromic subsets of substring **bca**. There are three valid subsets that form palindromic strings (**b**, **c**, and **a**), so we print the result of $3 \bmod (10^9 + 7) = 3$ on a new line.