

Self Balancing Tree

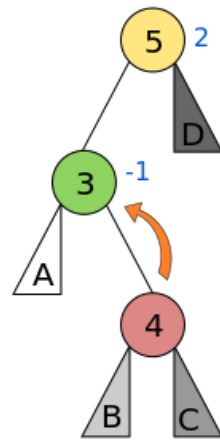
An AVL tree (Georgy Adelson-Velsky and Landis' tree, named after the inventors) is a self-balancing binary search tree. In an AVL tree, the heights of the two child subtrees of any node differ by at most one; if at any time they differ by more than one, rebalancing is done to restore this property.

We define balance factor for each node as :

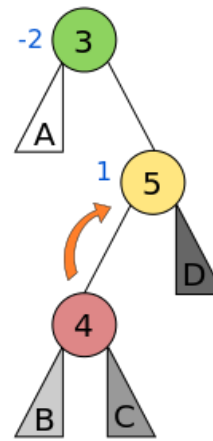
```
balanceFactor = height(left subtree) - height(right subtree)
```

The balance factor of any node of an AVL tree is in the integer range $[-1, +1]$. If after any modification in the tree, the balance factor becomes less than -1 or greater than $+1$, the subtree rooted at this node is unbalanced, and a rotation is needed.

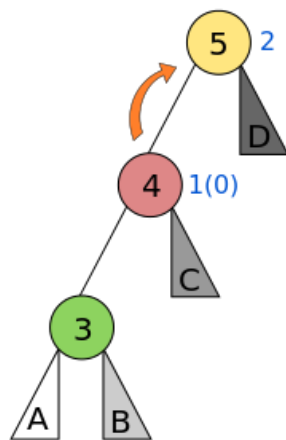
Left Right Case



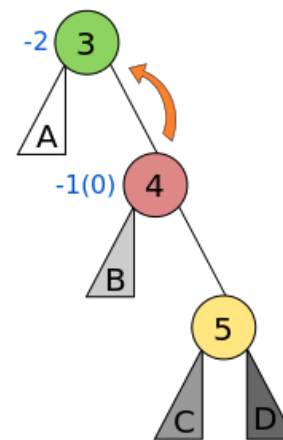
Right Left Case



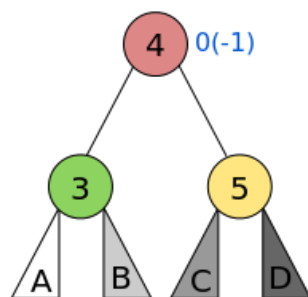
Left Left Case



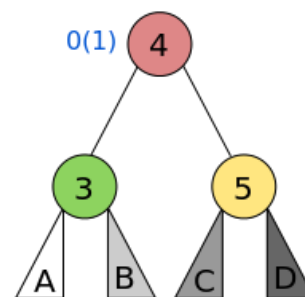
Right Right Case



Balanced



Balanced



(https://en.wikipedia.org/wiki/AVL_tree)

You are given a pointer to the root of an AVL tree. You need to insert a value into this tree and perform the necessary rotations to ensure that it remains balanced.

Input Format

You are given a function,

```
node *insert(node * root,int new_val)
{

}
```

'node' is defined as :

```
struct node
{
int val;           //value
struct node* left; //left child
struct node* right; //right child
int ht;           //height of the node
} node;
```

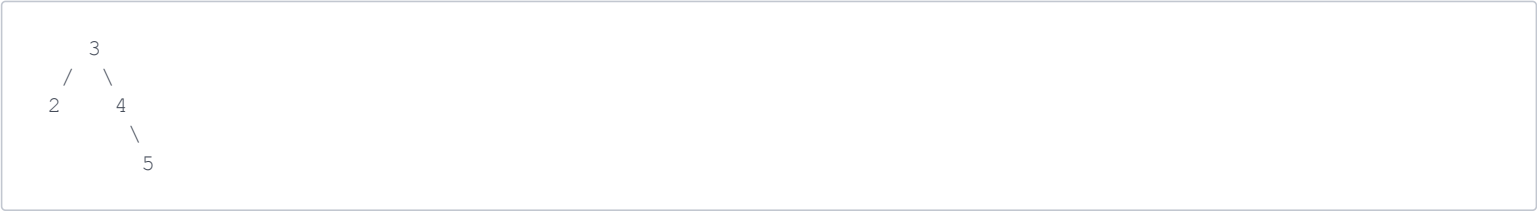
You only need to complete the function.

Note: All the values in the tree will be distinct. Height of a Null node is -1 and the height of the leaf node is 0.

Output Format

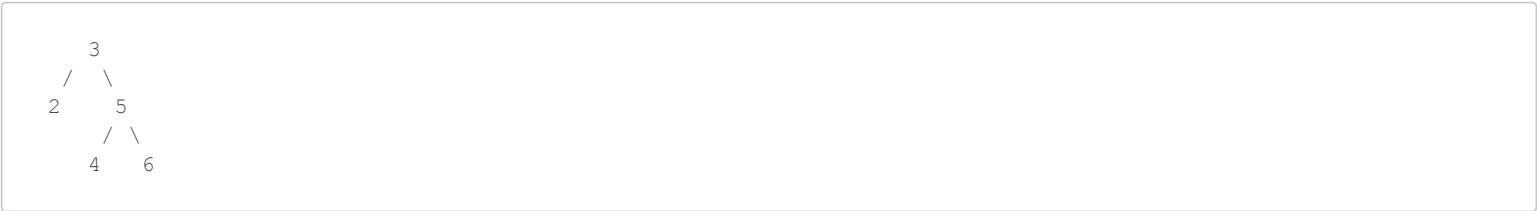
Insert the new value into the tree and return a pointer to the root of the tree. Ensure that the tree remains balanced.

Sample Input



The value to be inserted is 6.

Sample Output



Explanation

After inserting 6 in the tree. the tree becomes:



```

2      4 (Balance Factor = -2)
      \
       5 (Balance Factor = -1)
        \
         6 (Balance Factor = 0)

```

Balance Factor of nodes 3 and 4 is no longer in the range $[-1,1]$. We need to perform a rotation to balance the tree. This is the right right case. We perform a single rotation to balance the tree.

After performing the rotation, the tree becomes :

```

              3 (Balance Factor = -1)
            /   \
(Balance Factor = 0) 2       5 (Balance Factor = 0)
                  /   \
(Balance Factor = 0) 4       6 (Balance Factor = 0)

```