HackerRank

Project Euler #182: RSA encryption

This problem is a programming version of Problem 182 from projecteuler.net

The RSA encryption is based on the following procedure:

Generate two distinct primes p and q. Compute n = pq and $\phi = (p-1)(q-1)$. Find an integer e, $1 < e < \phi$, such that $\gcd(e, \phi) = 1$.

A message in this system is a number in the interval [0, n - 1]. A text to be encrypted is then somehow converted to messages (numbers in the interval [0, n - 1]). To encrypt the text, for each message, $m, c \equiv m^e \pmod{n}$ is calculated.

To decrypt the text, the following procedure is needed: calculate d such that $ed \equiv 1 \pmod{\phi}$, then for each encrypted message, c, calculate $m \equiv c^d \pmod{n}$.

There exist values of e and m such that $m^e \equiv m \pmod{n}$. We call messages m for which $m^e \equiv m \pmod{n}$ unconcealed messages.

An issue when choosing e is that there should not be too many unconcealed messages. For instance, let p = 19 and q = 37.

Then n=19 imes 37=703 and $\phi=18 imes 36=648$.

If we choose e=181, then, although $\gcd(181,648)=1$ it turns out that all possible messages m (

 $0 \leq m \leq n-1$) are unconcealed when calculating $m^e \pmod{n}$.

For any valid choice of e there exist some unconcealed messages.

It's important that the number of unconcealed messages is at a minimum.

For given p and q find the sum of all values of e, $1 < e < \phi(p,q)$ and $gcd(e,\phi) = 1$, so that the number of unconcealed messages for this value of e is at a minimum.

Input Format

Every test case contains a single line with two integers separated by a single space: p and q.

Constraints

p and q are distinct primes.

 $11 \le p,q \le 10^9.$

But for more than half of tests $11 \le p,q \le 10^6$.

Output Format

Output the sum of all values of e for which the number of unconcealed messages is at a minimum. As this number may be huge, output it modulo $10^9 + 7$.

Sample Input

1	1	13		

Sample Output

438

Explanation

The needed values of e are 23, 47, 59, 83, 107 and 119 which give us only 9 unconcealed messages.