

# Project Euler #233: Lattice points on a circle

This problem is a programming version of [Problem 233](#) from [projecteuler.net](#)

Let  $f(n)$  be the number of points with integer coordinates that are on a circle passing through  $(0, 0)$ ,  $(n, 0)$ ,  $(0, n)$  and  $(n, n)$ .

It can be shown that  $f(10000) = 36$ .

Given two integers  $N$  and  $m$ , what is the number of all positive integers  $n \leq N$  such that  $f(n) = 4m$ ?

## Input Format

The first line of each test file contains a single integer  $q$  which is the number of queries.  
Each of the next  $q$  lines contains two space-separated integers  $N$  and  $m$ .

## Constraints

- $1 \leq m \leq 200$ .
- $m$  is an odd squarefree integer.
- In testfiles 3 to 29:
  - $1 \leq q \leq 20$ .
  - $1 \leq N \leq 10^9$ .
- In testfile 30 and above:
  - $q = 1$ .
  - $1 \leq N \leq 5 \times 10^{10}$  when  $m = 3$ .
  - $1 \leq N \leq 10^{11}$  when  $m \neq 3$ .

## Output Format

Print the answer to each query on a new line.

## Sample Input 0

```
1
1000 1
```

## Sample Output 0

```
433
```

### Sample Input 1

```
1
1000000000000 87
```

### Sample Output 1

```
1
```

### Explanation 1

The only integer  $n$  less than  $10^{11}$  such that  $f(n) = 348$  is **79345703125**.

### Sample Input 2

```
1
1000000000000 31
```

### Sample Output 2

```
3
```

### Explanation 2

There exist only three integers  $n \leq 10^{11}$  such that  $f(n) = 124$ : **30517578125**, **61035156250** and **91552734375**.